

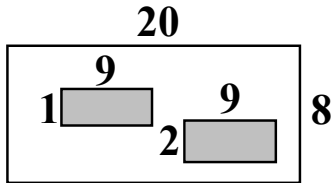
Geometric Probability

Up to this point, we have determined the probability of events, based solely on lists of information. Geometric probability is the probability of choosing a point at random from a specific area of space. Basically, it works like this:

$$\text{Geometric Probability} = \frac{(\text{Area of shape that I WANT})}{(\text{Area of outer shape, which is the TOTAL})}$$

First, we are going to practice determining area, as we will need that to determine probability.

EXAMPLE: What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?

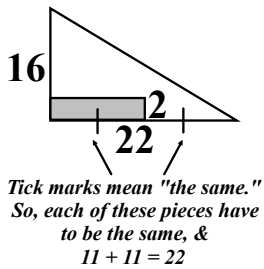


Sample Space	1 9	2 9	The rest of the outer shape (the big rectangle)
Amount (Area)	$bh = (9)(1) = 9$	$bh = (9)(2) = 18$	$\text{total} - (\text{rect's}) = 160 - (9 + 18) = 133$
Sample Size (Total)	$bh = (20)(8) = 160$	$\leftarrow \text{same} = 160$	$\leftarrow \text{same} = 160$
Probability	$\frac{9}{160}$	$\frac{18}{160} = \frac{9}{80}$	$\frac{133}{160}$

$$P(\text{Rectangle 1 or Rectangle 2}) = \frac{27}{160}$$

$$P(\text{NOT Rectangle 1 or Rectangle 2}) = \frac{133}{160}$$

EXAMPLE: What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?

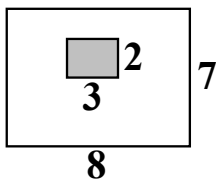


Sample Space	2 11 (must be 11 to be the same)	The rest of the outer shape (the big triangle)
Amount (Area)	$bh = (11)(2) = 22$	$\text{total} - \text{rectangle} = 176 - (22) = 154$
Sample Size (Total)	$\frac{bh}{2} = \frac{(16)(22)}{2} = 176$	$\leftarrow \text{same} = 176$
Probability	$\frac{22}{176} = \frac{11}{88} = \frac{1}{8}$	$\frac{154}{176} = \frac{7}{8}$

$$P(\text{Rectangle}) = \frac{1}{8}$$

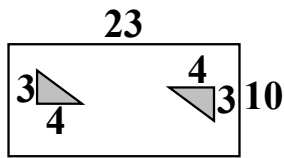
$$P(\text{NOT Rectangle}) = \frac{7}{8}$$

1. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?



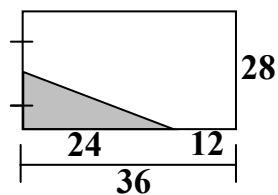
Sample Space	2 3	The rest of the total figure
Amount (Area)		
Sample Size	7	
Probability		

2. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?



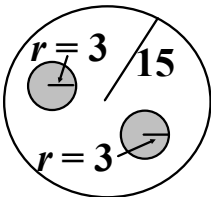
Sample Space			
Amount (Area)			
Sample Size			
Probability			

3. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?



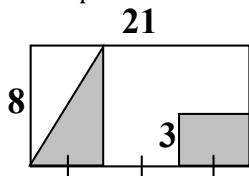
Sample Space			
Amount (Area)			
Sample Size			
Probability			

4. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement? (Use the area in terms of pi.)

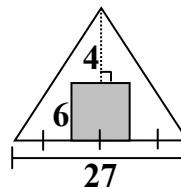


Sample Space	$r = 3$	$r = 3$	
Amount (Area)	$\pi r^2 =$	$\pi r^2 =$	
Sample Size			
Probability			

5. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?



6. What is the probability that a randomly selected point will be in the shaded part(s)? What is the probability of the complement?



Geometric Probability Answers

1. $\frac{3}{28}$	2. $\frac{6}{115}$	3. $\frac{1}{6}$
4. $\frac{2}{25}$	5. $\frac{7}{24}$	6. $\frac{2}{5}$