

Using Given Information to Write Quadratic Equations

Now that you are able to identify the parts on a quadratic graph ( $a, b, c, h, k, r_1$  &  $r_2$ ), you must be able to write a quadratic equation using those parts. There are 3 quadratic equation forms:

<p>Standard Form <math>f(x) = ax^2 + bx + c</math></p>	<p>Vertex Form <math>f(x) = a(x - h)^2 + k</math></p>	<p>Factored Form <math>f(x) = a(x - r_1)(x - r_2)</math></p>
<p>In this form, you simply plug in <math>a, b</math> &amp; <math>c</math> as they are - <u>make sure to bring their signs (+ -) with them.</u></p>	<p>In this form, you plug in <math>a</math> &amp; <math>k</math> as they are - <u>bringing their signs (+ -) with them.</u> But, when you plug in <math>h</math>, you <b>must switch</b> the sign.</p>	<p>In this form, you plug in <math>a</math> as it is - <u>bringing its sign (+ -) with it.</u> But, when you plug in the <math>r</math>'s, you <b>must switch</b> their signs.</p>
<p><b>Example:</b> <math>f(x) = \boxed{a}x^2 + \boxed{b}x + \boxed{c}</math>  <math>a = 3</math>  <math>b = -12</math>  <math>c = 9</math>  <math>h = 2</math>  <math>k = -3</math>  <math>r_1 = -3</math>  <math>r_2 = -1</math></p> <p><math>a = 3, b = -12, c = +9</math>  <math>f(x) = \boxed{3}x^2 - \boxed{12}x + \boxed{9}</math></p> <p>So, <b>standard form</b> is:  <math>f(x) = 3x^2 - 12x + 9</math></p>	<p><b>Example:</b> <math>f(x) = \boxed{a}(x - \boxed{h})^2 + \boxed{k}</math>  <math>a = 3</math>  <math>b = -12</math>  <math>c = 9</math>  <math>h = 2</math>  <math>k = -3</math>  <math>r_1 = -3</math>  <math>r_2 = -1</math></p> <p><math>a = 3, h = +2, k = -3</math>          Switched <math>h = -2!!</math>  <math>f(x) = \boxed{3}(x - \boxed{2})^2 - \boxed{3}</math></p> <p>So, <b>vertex form</b> is:  <math>f(x) = 3(x - 2)^2 - 3</math></p>	<p><b>Example:</b> <math>f(x) = \boxed{a}(x - \boxed{r_1})(x - \boxed{r_2})</math>  <math>a = 3</math>  <math>b = -12</math>  <math>c = 9</math>  <math>h = 2</math>  <math>k = -3</math>  <math>r_1 = -3</math>  <math>r_2 = -1</math></p> <p><math>a = 3, r_1 = -3, r_2 = -1</math>          Switched <math>r_1 = +3</math>          &amp; <math>r_2 = +1</math>  <math>f(x) = \boxed{3}(x + \boxed{3})(x + \boxed{1})</math></p> <p>So, <b>factored form</b> is:  <math>f(x) = 3(x + 3)(x + 1)</math></p>

For each set of quadratic information, write the quadratic in **standard form, vertex form and factored form.**

<p><b>EXAMPLE</b>  <math>a = -5</math>  <math>b = -40</math>  <math>c = -3</math>  <math>h = 4</math>  <math>k = 5</math>  <math>r_1 = 3</math>  <math>r_2 = 5</math></p> <p><b>Standard Form:</b>  <math>f(x) = ax^2 + bx + c</math>  <math>f(x) = -5x^2 - 40x - 3</math></p> <p><b>Vertex Form:</b> <i>switch h's sign (but not k's)!</i>  <math>f(x) = a(x - h)^2 + k</math>  <math>f(x) = -5(x - 4)^2 + 5</math></p> <p><b>Factored Form:</b> <i>switch the signs for <math>r_1</math> &amp; <math>r_2</math>!</i>  <math>f(x) = a(x - r_1)(x - r_2)</math>  <math>f(x) = -5(x - 3)(x - 5)</math></p>	<p>1.  <math>a = -1</math>  <math>b = -6</math>  <math>c = -5</math>  <math>h = -3</math>  <math>k = 4</math>  <math>r_1 = -5</math>  <math>r_2 = -1</math></p> <p><b>Standard Form:</b></p> <p><b>Vertex Form:</b></p> <p><b>Factored Form:</b></p>
<p>2.  <math>a = -3</math>  <math>b = 0</math>  <math>c = 3</math>  <math>h = 0</math>  <math>k = 3</math>  <math>r_1 = -1</math>  <math>r_2 = 1</math></p> <p><b>Standard Form:</b></p> <p><b>Vertex Form:</b></p> <p><b>Factored Form:</b></p>	<p>3.  <math>a = 2</math>  <math>b = 8</math>  <math>c = 8</math>  <math>h = -2</math>  <math>k = 0</math>  <math>r_1 = -2</math>  <math>r_2 = -2</math></p> <p><b>Standard Form:</b></p> <p><b>Vertex Form:</b></p> <p><b>Factored Form:</b></p>
<p>4.  <math>a = -2</math>  <math>b = 4</math>  <math>c = 6</math>  <math>h = -1</math>  <math>k = 8</math>  <math>r_1 = -3</math>  <math>r_2 = 1</math></p> <p><b>Standard Form:</b></p> <p><b>Vertex Form:</b></p> <p><b>Factored Form:</b></p>	<p>5.  <math>a = 1</math>  <math>b = 2</math>  <math>c = -8</math>  <math>h = -1</math>  <math>k = -9</math>  <math>r_1 = -4</math>  <math>r_2 = 2</math></p> <p><b>Standard Form:</b></p> <p><b>Vertex Form:</b></p> <p><b>Factored Form:</b></p>

<p>6.</p> <p><math>a = 3</math>      <b>Standard Form:</b>  <math>b = -6</math>  <math>c = -9</math>  <math>h = 1</math>      <b>Vertex Form:</b>  <math>k = -12</math>  <math>r_1 = -1</math>  <math>r_2 = 3</math></p> <p><b>Factored Form:</b></p>	<p>7.</p> <p><math>a = -1</math>      <b>Standard Form:</b>  <math>b = 0</math>  <math>c = 4</math>  <math>h = 0</math>      <b>Vertex Form:</b>  <math>k = 4</math>  <math>r_1 = -2</math>  <math>r_2 = 2</math></p> <p><b>Factored Form:</b></p>
<p>8.</p> <p><math>a = 2</math>      <b>Standard Form:</b>  <math>b = 0</math>  <math>c = -8</math>  <math>h = 0</math>      <b>Vertex Form:</b>  <math>k = -8</math>  <math>r_1 = -2</math>  <math>r_2 = 2</math></p> <p><b>Factored Form:</b></p>	<p>9.</p> <p><math>a = 3</math>      <b>Standard Form:</b>  <math>b = -6</math>  <math>c = 3</math>  <math>h = 1</math>      <b>Vertex Form:</b>  <math>k = 0</math>  <math>r_1 = 1</math>  <math>r_2 = 1</math></p> <p><b>Factored Form:</b></p>
<p>10.</p> <p><math>a = 4</math>      <b>Standard Form:</b>  <math>b = 40</math>  <math>c = 84</math>  <math>h = -5</math>      <b>Vertex Form:</b>  <math>k = -16</math>  <math>r_1 = -7</math>  <math>r_2 = -3</math></p> <p><b>Factored Form:</b></p>	<p>11.</p> <p><math>a = -7</math>      <b>Standard Form:</b>  <math>b = -42</math>  <math>c = -63</math>  <math>h = -3</math>      <b>Vertex Form:</b>  <math>k = 0</math>  <math>r_1 = -3</math>  <math>r_2 = -3</math></p> <p><b>Factored Form:</b></p>
<p>12.</p> <p><math>a = 5</math>      <b>Standard Form:</b>  <math>b = -40</math>  <math>c = 75</math>  <math>h = 4</math>      <b>Vertex Form:</b>  <math>k = -5</math>  <math>r_1 = 3</math>  <math>r_2 = 5</math></p> <p><b>Factored Form:</b></p>	<p>13.</p> <p><math>a = -10</math>      <b>Standard Form:</b>  <math>b = -40</math>  <math>c = 0</math>  <math>h = 2</math>      <b>Vertex Form:</b>  <math>k = 40</math>  <math>r_1 = 0</math>  <math>r_2 = 4</math></p> <p><b>Factored Form:</b></p>