

Simplifying Exponents

Exponents are relatively simple to deal with, assuming that you know the rules. Here are a few of them:

- 1) If your exponent is 0, then the base (the number or variable that has an exponent on it) becomes 1.
(example: $4,719^0 = 1$)
- 2) If your exponent is 1, then the exponent disappears, and you're left with the base as is.
(example: $329^1 = 329$)

Example	Your Turn	Still Your Turn
$4^0 = 1$ <i>Any number to the power of 0 = 1.</i>	1. 7^0	2. 9^0
$a^0 = 1$ <i>Any number to the power of 0 = 1.</i>	3. g^0	4. h^0
$5^1 = 5$ <i>Any number to the power of 1 = base number.</i>	5. 3^1	6. 18^1
$r^1 = r$ <i>Any number to the power of 1 = base number.</i>	7. b^1	8. q^1
$\frac{a^0 b^1 c^1 d^1}{b^1 d^0} = \frac{(1)bcd}{b(1)}$ $= \frac{bcd}{b}$ $= cd$ <i>Start with numbers to exponent of 0-those become 1.</i> <i>*b cancels ÷b</i>	9. $\frac{p^1 r^0 t^1}{t^1 y^0}$	10. $\frac{s^0 w^1 e^1}{e^1 t^0}$

- 3) If your exponent is negative, then the base flips from the top to the bottom of a fraction or from the bottom to the top. The exponent becomes positive and moves with its base.

(examples: $6^{-3} = \frac{1}{6^{+3}}$ or $\frac{1}{7^{-2}} = 7^2$)

Tip: Before you deal with any other part of the exponent problem, getting rid of the negative by flipping the base.

$4^{-1} = \frac{1}{4^1} = \frac{1}{4}$ <i>The negative exponent flips the base (4^1) from the top to the bottom. $4^1 = 4$</i>	11. 3^{-1}	12. 8^{-1}
$\frac{1}{5^{-1}} = 5^1 = 5$ <i>The negative exponent flips the base (5^1) from the bottom to the top. $5^1 = 5$</i>	13. $\frac{1}{9^{-1}}$	14. $\frac{1}{6^{-1}}$
$2^{-2} = \frac{1}{2^2} = \frac{1}{4}$ <i>The negative exponent flips the base (2^2) from the top to the bottom. $2^2 = 4$</i>	15. 5^{-3}	16. 3^{-5}
$a^{-5} = \frac{1}{a^5}$ <i>The negative exponent flips the base (a^5) from the top to the bottom.</i>	17. c^{-8}	18. x^{-20}
$\frac{1}{a^4 p^{-2}} = \frac{p^2}{a^4}$ <i>The negative exponent flips the base (p^2) from the bottom to the top.</i>	19. $\frac{1}{s^{-9} t^2}$	20. $\frac{1}{q^{-7} r^3}$
$\frac{a^{-4}}{b^{-2} c^3} = \frac{b^2}{a^4 c^3}$ <i>The negative exponent flips the top base (a^4) from the top to the bottom, and the bottom base (b^2) from the bottom to the top.</i>	21. $\frac{m^{-2}}{r^3 s^{-5}}$	22. $\frac{x^5 y^{-2}}{z^8}$

- 4) If you have bases with exponents being **multiplied** together, **and the bases are the same**, then you leave the base as it is and add the exponents.
 (example: $5^7 5^3 = 5^{7+3}$)
- 5) If you have bases with exponents being **divided**, **and the bases are the same**, then subtract the exponents (bigger - smaller) and leave the base (with its new exponent) where the bigger exponent started.

(examples: $\frac{4^2}{4^5} = \frac{1}{4^{5-2}}$ or $\frac{9^7}{9^6} = \frac{9^{7-6}}{1}$)

- 6) If you have an exponent on the outside of a set of parentheses, then you share that exponent with every base in the parentheses. To do this, you multiply each exponent inside by the shared exponent. Don't forget, though: just because you don't see an exponent doesn't mean it isn't there. The invisible exponent is always 1.

<p><i>add exponents</i></p> $4^{24^3} = 4^{2+3}$ $= 4^5$ $= 4 \times 4 \times 4 \times 4 \times 4$ $= 16 \times 16 \times 4$ $= 256 \times 4$ $= 1024$	23. 9^{29^1}	24. $2^{3^2^2}$
$b^2 b^{19} c^3 = b^{2+19} c^3$ $= b^{21} c^3$	25. $d^2 a^3 d^8$	26. $h^3 p^2 h^3 t$
<p><i>subtract exponents</i></p> $\frac{x^2 y^5}{xz^5} = \frac{xy^5}{z^5}$	27. $\frac{a^3 b^7}{b^5 c^2}$	28. $\frac{g^2 h^5}{fh^3}$
<p><i>multiply exponents</i></p> $(a^3 b^2)^5 = a^{3(5)} b^{2(5)}$ $= a^{15} b^{10}$	29. $(x^2 y^4)^8$	30. $(m^7 n^2 p^4)^3$
<p><i>multiply exponents</i></p> $\frac{a^3 d^0}{b^2 d^2} = \frac{a^3}{b^2 d^2}$ $= \frac{a^{3(7)}}{b^{2(7)} d^{1(7)}}$ $= \frac{a^{21}}{b^{14} d^7}$	31. $\frac{x^3 y^5 z^2}{xy^3 z^4}$	32. $\frac{m^2 n^7 p^3}{n^5 p^4}$

Now, you are going to apply everything we've just learned, on your own.

Tip: Deal with negative exponents first, then with exponents of 0 or 1. Next, simplify inside the parentheses before dealing with the outside exponent.

33. $\frac{a^0 b^5 b^2 c^1}{b^6 d^{-3}}$	34. $\frac{x^3 y^{-5}}{x^{-2} y^0}$	35. $\frac{p^0 r^{-2} s^5 s^6}{s^3}$
36. $(a^4 b^{-3} c^2 a^5 d^0)^3$	37. $(m^3 n^2 p^3 m^5)^0$	38. $(x^6 x^{-2} y^5 z^1 y^0)^5$