

Name: _____

Solving Permutations and Combinations

The most important part of determining permutations and combinations is knowing which formula to use.

| Permutation Formula (when order matters) | Combination Formula (when order doesn't matter) |
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| $\frac{n!}{(n-r)!}$ <p><i>n = total number of items & r = number of items wanted</i></p> <p>EX: How many ways can you choose first, second, and third place out of a group of 5 players?</p> <p><i>It's a permutation, because order matters (1st is different from 2nd). n = total = 5 players r = wanted = 3 winners</i></p> $\frac{n!}{(n-r)!} = \frac{5!}{(5-3)!} = \frac{5 \cdot 4 \cdot 3 \cdot \cancel{2!}}{\cancel{2!}} = 5 \cdot 4 \cdot 3 = \boxed{60}$ | $\frac{n!}{(n-r)!r!}$ <p><i>n = total number of items & r = number of items wanted</i></p> <p>EX: How many ways can you choose a set of 3 winners out of 5 applicants to get a \$50 gift card?</p> <p><i>It's a combination, because order doesn't matter (they all get the same gift card). n = total = 5 players r = wanted = 3 winners</i></p> $\frac{n!}{(n-r)!r!} = \frac{5!}{(5-3)!3!} = \frac{5 \cdot 4 \cdot \cancel{3!}}{2 \cdot 1 \cdot \cancel{3!}} = \frac{20}{2} = \boxed{10}$ |

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| 1. How many ways can you choose 8 songs out of 12 to put on a playlist? | 2. How many ways can you arrange 2 paintings on the wall, if you have 6 paintings to choose from? | 3. How many ways can you arrange 9 players in a batting order if there are 12 total players? |
| 4. How many ways can you choose a team of 5 players, if the players are selected at random from a group of 10? | 5. How many ways can you watch 3 movies, if you have 12 possible movies to watch? | 6. How many ways can you buy 6 books, if your pile of options has 8 books in it? |
| 7. How many groups of recordings are possible if you choose 2 shows to record out of 20 options? | 8. How many ways can you pack 7 shirts for a vacation if there are 11 shirt options? | 9. How many ways can you organize 5 appointments in a schedule, if you schedule 5 total appointments? <i>Hint: It's possible to have a 0!. Like with an exponent of 0, it just equals 1.</i> |

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| <p>10. How many ways can you award 1st, 2nd, 3rd, and 4th place trophies if 9 people competed?</p> | <p>11. How many possibilities are there when you buy two chairs out of 11 possible options to put in the living room?</p> | <p>12. How many possibilities are there for choosing a group of 8 students to participate in a rally?</p> |
| <p>13. How many ways are there to play 12 songs from a playlist of 15?</p> | <p>14. How many ways are there to buy 4 video games from a stack of 10 choices?</p> | <p>15. How many possibilities are there to choose a President and Vice President from a set of 4 candidates?</p> |
| <p>16. How many ways can you eat 6 out of 8 candy bars, if you eat them one after the other?</p> | <p>17. How many possible ways are there to choose 3 out of 7 friends to go to a concert with you?</p> | <p>18. How many possibilities are there for 5 pens to randomly chosen out of a bag of 10 pens, if they are all chosen in one bunch?</p> |
| <p>19. How many ways can 3 songs be played on a guitar if the guitarist knows 15 songs?</p> | <p>20. How many ways can 6 pictures be displayed on a bookshelf, if there are 9 pictures to choose from?</p> | <p>21. How many ways can the top 2 students, out of 30, be chosen to receive a homework pass?</p> |