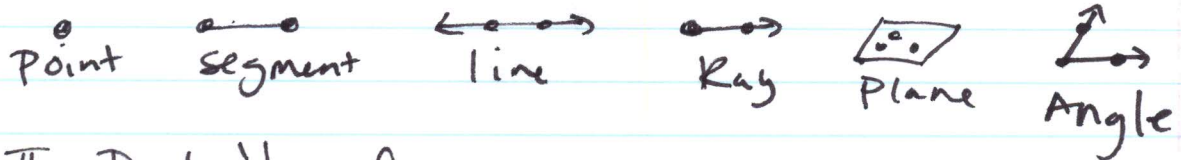


1-1 Basic Figures & Their Names

I. Basic Figures



II. Details of a...

A. point 1. looks like: •

2. Needs 1 pt

3. ~~are~~ named with 1 letter

ex/ • T ... Point T
a.k.a. "T"

B. Segment


1. looks like:



NOT A
LINE B/C
IT STOPS

2. Needs 2 points & is straight

3. named with 2 letters & a segment hat -

ex/  \overline{AM} or \overline{MA}

4. to write its measure or length, take off the hat!


ex/



LENGTH:
 $MA = 3$

NAMES:
 \overline{MA} or \overline{AM}

C. Line

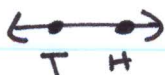
1. looks like 

NEVER
STOPS


2. Needs 2 points, ~~is~~ is straight, & goes on forever




3. NAMED with 2 letters & a line hat or its nickname

ex/



\overleftrightarrow{TH} or \overleftrightarrow{HT}

D. Ray

1. looks like  or  or  one
one
2. Needs 1 endpoint where it STARTS & 1 through point.
3. Name with 2 letters (START WITH ENDPNT!) & a ray hat (always \rightarrow)

ex/



\overrightarrow{SI}


NOT

~~\overrightarrow{IS}~~

~~OR \overleftarrow{IS}~~

~~OR \overleftarrow{SI}~~

E. Plane

1. looks like 
2. Needs 3 pts & is a flat surface
not in a line!
(NON COLLINEAR)
3. Name with 3 points & \square symbol out front
or nickname!

ex/



\square AWE

\square WAE

\square EAW


OR \square S

\square AEW

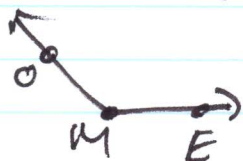
\square WEA

\square EWA

F. Angle

1. looks like 
2. Needs 3 pts (corner pt called "vertex") & bends into 2 straight paths w/ \rightarrow s
3. Name with 3 letters OR corner letter & \angle symbol out front

ex/



$\angle OME$

$\angle MEO$

$\angle EOM$

OR $\angle M$

$\angle OEM$

$\angle MOE$

$\angle EMO$

4. To write "measure of...", stick an "m" before the symbol.



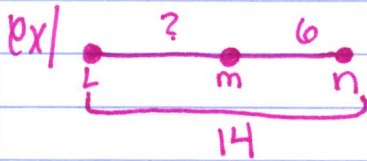
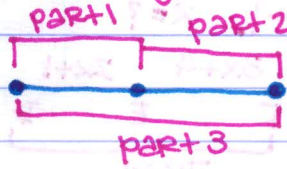
$\cong m\angle OME$ OR $m\angle M$ etc.

Segment Addition

(when you add connected segments)



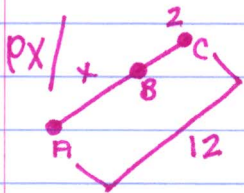
I. How to add 'em:
part 1 + part 2 =
Whole



$$LM + MN = LN$$

$$? + 6 = 14$$

$$? = 8$$

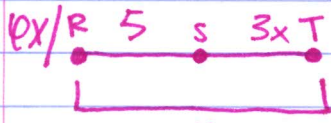


$$x + 2 = 12$$

$$x = 10$$

$$AB = 10$$

$$AB + BC = AC$$

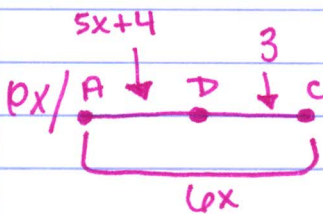


$$5 + 3x = 11$$

$$-5 \quad -5$$

$$\frac{3x}{3} = \frac{6}{3}$$

$$x = 2$$



$$AD + DC = AC$$

$$(5x+4) + 3 = 6x$$

$$5x + 7 = 6x$$

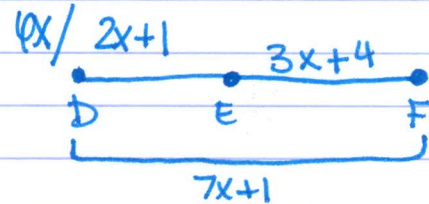
$$7 = x$$

$$AD = 5(x+4) = 5(7) + 4$$

$$= 35 + 4$$

$$= 39$$

$$AC = 6x = 6(7) = 42$$



$$DE + EF = DF$$

$$(2x+1) + (3x+4) = 7x+1$$

$$5x+5 = 7x+1$$

$$DE = 2x+1 \quad 5 = 2x+1$$

$$= 2(2)+1 = 5 \quad \frac{4}{2} = \frac{2x}{2}$$

$$EF = 3x+4 \quad 2 = 2$$

$$= 3(2)+4 = 10 \quad 2 = x$$

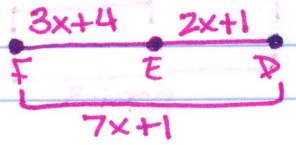
$$DF = 7x+1$$

$$= 7(2)+1 = 15$$

Ex/ E is between D and F.

DE is $2x+1$, EF is $3x+4$ and

DF is $7x+1$. $x=?$



$FE + ED = FD$

$(3x+4) + (2x+1) = 7x+1$

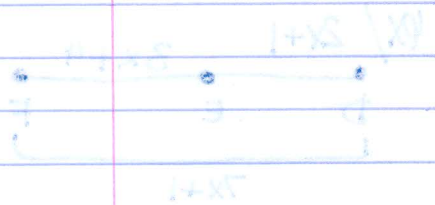
$5x+5 = 7x+1$

$5x+4 = 7x$

$4 = 2x$

$2 = x$

$x = 2$



$DE + EF = DF$

$(2x+1) + (3x+4) = 7x+1$

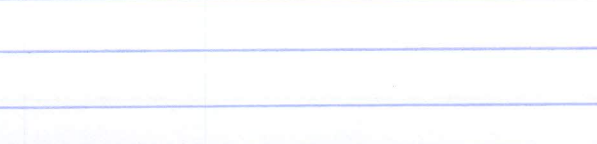
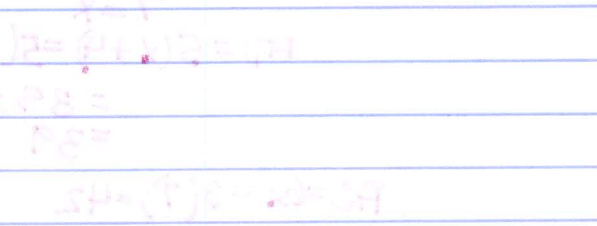
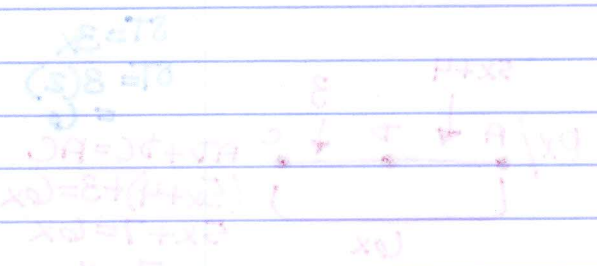
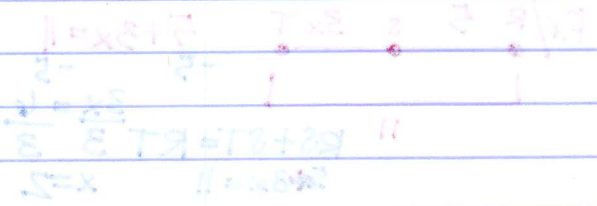
$5x+5 = 7x+1$

$4x+4 = 2x$

$2(x+2) = 2x$

$x+2 = x$

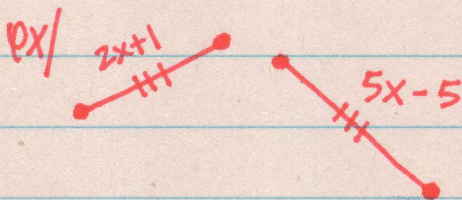
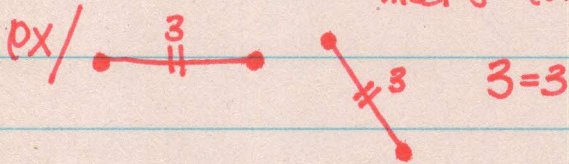
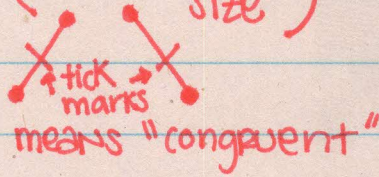
$2 = 0$



Congruent Segments

I. Congruent (same shape size)

\cong



$$2x+1 = 5x-5$$

$$1 = 3x-5$$

$$6 = 3x$$

$$2 = x$$

$$2x+1 = 2(2)+1$$

$$= 4+1$$

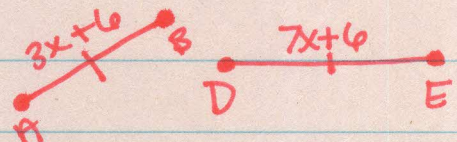
$$= 5$$

Px/ $AB = 3x+6$ & $DE = 7x-6$

$DE = ?$

$\overline{AB} \cong \overline{DE}$

$AB = DE$



$$DE = 7x-6$$

$$= 7(3)-6$$

$$= 21-6$$

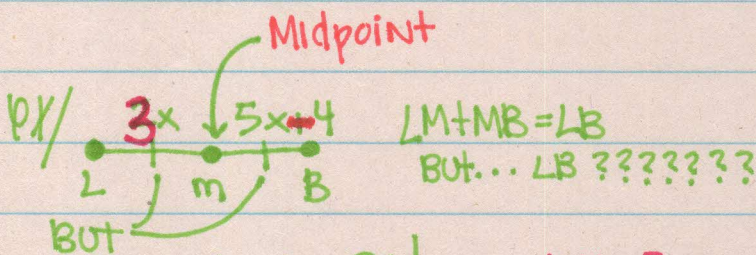
$$= 15$$

$$3x+6 = 7x-6$$

$$6 = 4x-6$$

$$12 = 4x$$

$$3 = x$$



They're \cong !

$\overline{LM} \cong \overline{MB}$

$LM = MB$

$3x = 5x-4$

$-2x = -4$

$x = \frac{4}{2} = 2$

$LM = 3x$

$LM = 3(2)$

$= 6$

$MB = 5(2)-4$

$MB = 6$

$LM + MB = LB$

$6 + 6 = LB$

$12 = LB$

SAME!!!

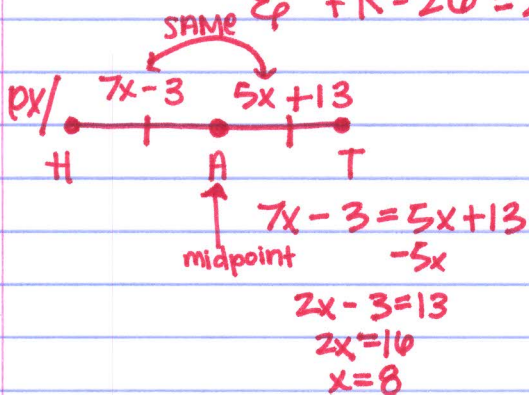
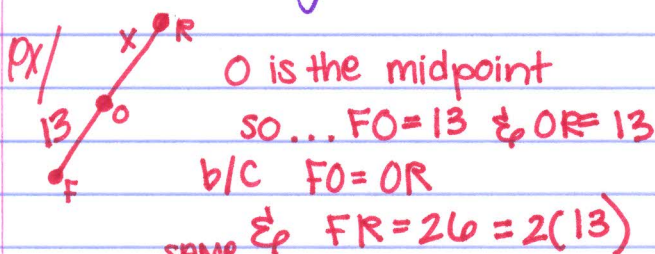
Midpoints and Congruence

I. Midpoints (Bisectors)

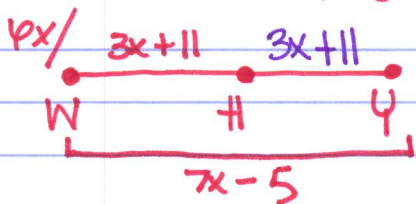
A the point in the middle (EXACTLY)



- creates 2 equal segments!
- the whole segment is 2 times 1 apart!



$$\begin{aligned} HA &= 7(8) - 3 \\ &= 56 - 3 \\ HA &= 53 \rightarrow AT = 53 \\ HT &= 53 + 53 = 106 \end{aligned}$$



H is the midpoint $x = 27$

$$\begin{aligned} WH &= 3(27) + 11 = 81 + 11 \\ WH &= 92 \\ WY &= 184 \\ HY &= 92 \end{aligned}$$

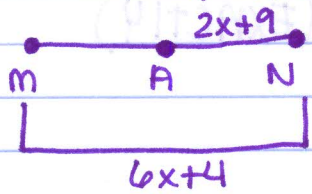
because H is the midpoint
we know $WH = HY$
now H's segment addition:
 $3x + 11 + 3x + 11 = 7x - 5$
 $6x + 22 = 7x - 5$

we know

$$\begin{aligned} 2(WH) &= WY \\ 2(3x + 11) &= 7x - 5 \\ 6x + 22 &= 7x - 5 \\ 22 &= x - 5 \\ 27 &= x \end{aligned}$$

px/ A is the midpoint of \overline{MN}

$AN = 2x+9$ & $\overline{MN} = 6x+4$ $MA = ?$



$$2(2x+9) = 6x+4$$

$$4x+18 = 6x+4$$

$$-4 = 2x+4$$

$$\frac{14}{2} = \frac{2x}{2}$$

$$MA = 2x+9$$

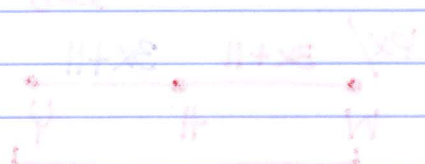
$$2(7)+9$$

$$= 14+9 = 23$$

Faint handwritten notes in red ink, possibly related to the midpoint formula or algebraic steps.



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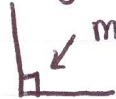
Faint handwritten notes in red ink, possibly related to the midpoint formula or algebraic steps.

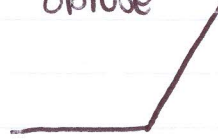
Angles and Addition

I. Types of Angles

Acute

 smaller than 90°

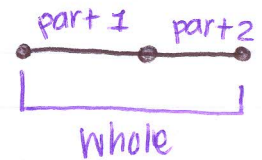
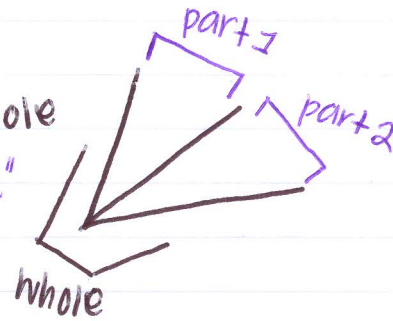
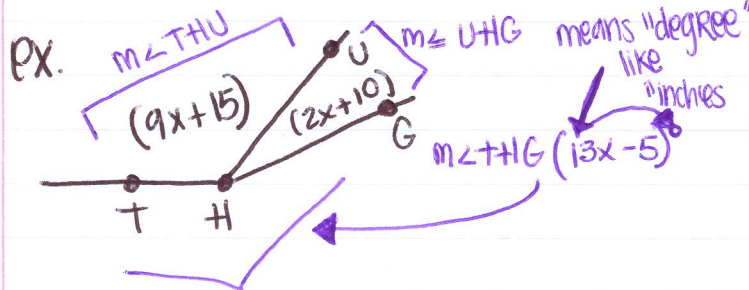
Right

 measures 90°

obtuse

 bigger than 90°


 exactly 180°

II. Angle Addition

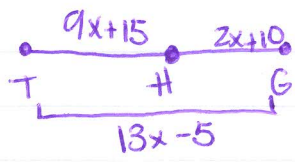
part 1 + part 2 = whole



$$\begin{aligned}
 m\angle THU + m\angle UHG &= m\angle THG \\
 9x + 15 + 2x + 10 &= 13x - 5 \\
 11x + 25 &= 13x - 5 \\
 25 &= 2x - 5 \\
 30 &= 2x \\
 15 &= x
 \end{aligned}$$

$$\begin{aligned}
 m\angle THU &= 9(15) + 15 = 150 \\
 m\angle UHG &= 2(15) + 10 = 30 + 10 = 40 \\
 m\angle THG &= 13(15) - 5 = 195 - 5 = 190
 \end{aligned}$$

think of it like:



1-3

Segments vs. Angles & their Measures

I. Types of Acute
less than Right

Right
means 90°
Exactly 90°

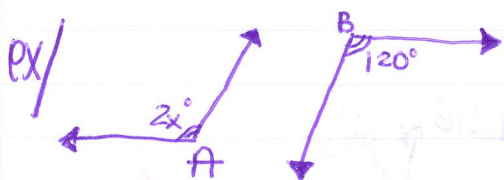
obtuse
more than Right
bigger than 90°

straight
exact, 180°

II. Congruence \cong

Segments
mean \cong (congruence)

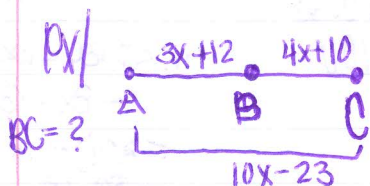
Angles
curves mean \cong



$$\begin{aligned} \angle A &\cong \angle B \\ m\angle A &= m\angle B \\ 2x &= 120^\circ \\ x &= 60^\circ \\ m\angle A &= 120^\circ \end{aligned}$$

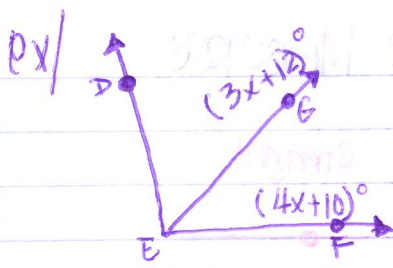
III. Addition Segment

part 1 + part 2 = whole



$$\begin{aligned} AB + BC &= AC \\ 3x + 12 + 4x + 10 &= 10x - 23 \\ 7x + 22 &= 10x - 23 \\ 22 &= 3x - 23 \\ 45 &= 3x \\ 15 &= x \end{aligned}$$

$$\begin{aligned} BC &= 4(15) + 10 \\ &= 60 + 10 \\ &= 70 \end{aligned}$$



$$m\angle DEF = (10x - 23)^\circ$$

$$m\angle GEF = ?$$

part 1 + part 2 = whole

$$m\angle DEG + m\angle GEF = m\angle DEF$$

$$(3x + 12) + (4x + 10) = (10x - 23)$$

same as before

$$7x + 22 = 10x - 23$$

$$22 = 3x - 23$$

$$\frac{45}{3} = \frac{3x}{3}$$

$$x = 15$$

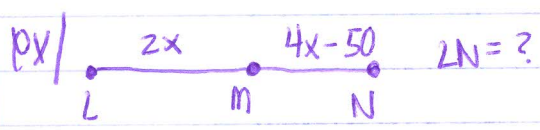
$$m\angle GEF = 4(15) + 10$$

$$= 60 + 10$$

$$= 70^\circ$$

IV. Midpoints & Bisectors

part 1 = part 2 OR 2(part) = whole



M is midpoint

$$LM = MN$$

$$2x = 4x - 50$$

$$-4x \quad -4x$$

$$-2x = -50$$

$$x = 25$$

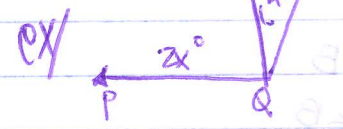
~~LN~~
$$MN = 4(25) - 50$$

$$= 100 - 50$$

$$= 50$$

$$LM = 50$$

$$LN = 100$$



RQ bisects $\angle PQR$

$$m\angle PQR = ?$$

$$\angle PQR = m\angle RQS$$

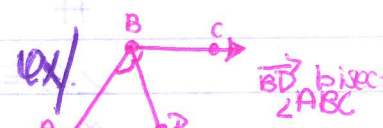
$$2x = 4x - 50$$

$$-2x = -50$$

$$x = 25$$

$$m\angle PQR = m\angle RQS$$

$$= 50 + 50 = 100^\circ$$



BD bisects $\angle ABC$

$$m\angle ABD = (8x - 18)$$

$$m\angle ABC = (10x + 30)^\circ \text{ whole}$$

$$m\angle DBC = ?$$

$$2(\text{part}) = \text{whole}$$

$$2(m\angle ABD) = m\angle ABC$$

$$2(8x - 18) = (10x + 30)$$

$$16x - 36 = 10x + 30$$

$$6x - 36 = 30$$

$$6x = 66$$

$$x = 11$$

$$m\angle DBC = m\angle ABD$$

$$= 8x - 18$$

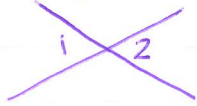
$$= 8(11) - 18$$

$$= 88 - 18$$

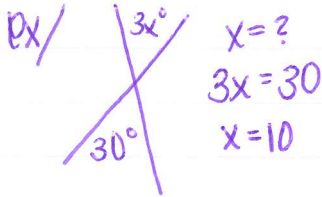
$$= 70^\circ$$

Angle Pairs

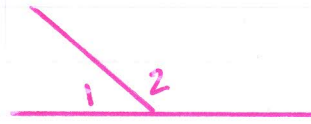
Vertical
look like:



$\angle 1$ & $\angle 2$ are
vertical
they're equal!
 $m\angle 1 = m\angle 2$

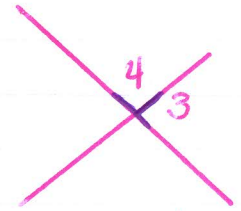


Linear Pair



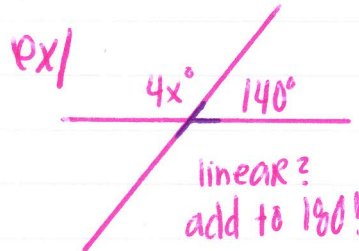
$\angle 1$ and $\angle 2$
are linear

OR



$\angle 4$ and $\angle 3$ are
linear.

add to = 180° !



$$4x + 140 = 180$$

$$4x = 40$$

$$x = 10^\circ$$

Complementary Angles

(No picture)

2 angles + = 90°

ex/ $m\angle 1 = 40^\circ$ & $m\angle 2 = 50^\circ$
 $40 + 50 = 90$

Complementary
Add to 90 !

ex/ $\angle 3$ & $\angle 4$ are complementary
 $m\angle 3 = 10x$ $m\angle 4 = 8x$ $x = ?$
 $10x + 8x = 90$
 $18x = 90$
 $x = 5$

Supplementary

(No picture)

2 angles + = 180°
(Linear pair is supp.)

ex/ $m\angle 7 = 102^\circ$ & $m\angle 8 = 78^\circ$
 $102 + 78 = 180$

102 / 78

Supplementary
add = 180 !

ex/ $\angle 9$ & $\angle 10$ are supplementary
 $m\angle 9 = 10x$ $m\angle 10 = 8x$ $x = ?$
 $10x + 8x = 180$
 $x = 10$